

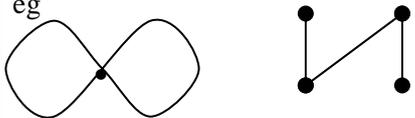
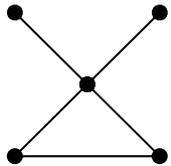
4736

Mark Scheme

June 2009

4736 Decision Mathematics 1

1 (i)	[43 172 536 17 314 462 220 231] 43 172 536 17 220 314 462 231	M1 M1 A1	First folder correct Second folder correct All correct (cao)	[3]
(ii)	536 462 314 231 220 172 43 17 536 462 314 231 220 172 43 17	B1 M1 A1	List sorted into decreasing order seen (cao) [Follow through from a decreasing list with no more than 1 error or omission] First folder correct All correct	[3]
(iii)	$(5000 \div 500)^2 \times 1.3$ = 130 seconds	M1 A1	$10^2 \times 1.3$ or any equivalent calculation Correct answer, with units	[2]
Total = 8				

2 (i)	The sum of the orders must be even, (but $1+2+3+3 = 9$ which is odd).	B1	There must be an even number of odd nodes.	[1]
(ii) a	eg 	M1 A1	A graph with five vertices that is neither connected nor simple Vertex orders 1, 1, 2, 2, 4	[2]
b	Because it is not connected	B1	You cannot get from one part of the graph to the other part.	[1]
c	eg 	B1	A connected graph with vertex orders 1, 1, 2, 2, 4 (Need not be simple)	[1]
(iii) a	There are five arcs joined to A. Either Ann has met (at least) three of the others or she has met two or fewer, in which case there are at least three that she has not met. In the first case at least three of the arcs joined to A are blue, in the second case at least three of the arcs joined to A are red.	M1 A1	A reasonable attempt (for example, identifying that there are five arcs joined to A) A convincing explanation (this could be a list of the possibilities or a well reasoned explanation)	[2]
b	If any two of Bob, Caz and Del have met one another then B, C and D form a blue triangle with A. Otherwise B, C and D form a red triangle.	M1 A1	A reasonable or partial attempt (using A with B, C, D) A convincing explanation (explaining both cases fully)	[2]
Total = 9				

<p>3 (i)</p>	$y \geq x$ $x + y \leq 8$ $x \geq 1$	<p>M1 M1 M1 A1</p>	<p>Line $y = x$ in any form Line $x + y = 8$ in any form Line $x = 1$ in any form All inequalities correct [Ignore extra inequalities that do not affect the feasible region]</p>	<p>[4]</p>
<p>(ii)</p>	<p>(1, 1), (1, 7), (4, 4)</p>	<p>M1 A1</p>	<p>Any two correct coordinates All three correct [Extra coordinates given \Rightarrow M1, A0]</p>	<p>[2]</p>
<p>(iii)</p>	<p>(1, 7) 23 (4, 4) 20 At optimum, $x = 1$ and $y = 7$ Maximum value = 23</p>	<p>M1 A1 A1</p>	<p>Follow through if possible Testing vertices or using a line of constant profit (may be implied) Accept (1, 7) identified 23 identified</p>	<p>[3]</p>
<p>(iv)</p>	<p>$2 \times 1 + k \times 7 \geq 2 \times 4 + k \times 4$ $k \geq 2$</p>	<p>M1 A1</p>	<p>$2 + 7k$ or implied, or using line of gradient $-\frac{2}{k}$ Greater than or equal to 2 (cao) [$k > 2 \Rightarrow$ M1, A0]</p>	<p>[2]</p>
<p>Total = 11</p>				

<p>4 (i)</p>	<div style="display: flex; justify-content: space-around; align-items: flex-start;"> <div style="text-align: center;"> <table border="1" style="margin-bottom: 5px;"> <tr><td>1</td><td>0</td></tr> <tr><td colspan="2" style="height: 15px;"></td></tr> </table> <p>A</p> </div> <div style="text-align: center;"> <table border="1" style="margin-bottom: 5px;"> <tr><td>6</td><td>8</td></tr> <tr><td colspan="2" style="height: 15px;"></td></tr> </table> <p>E</p> </div> </div> <div style="display: flex; justify-content: space-around; align-items: flex-start; margin-top: 10px;"> <div style="text-align: center;"> <table border="1" style="margin-bottom: 5px;"> <tr><td>2</td><td>2</td></tr> <tr><td colspan="2" style="height: 15px;"></td></tr> </table> <p>B</p> </div> <div style="text-align: center;"> <table border="1" style="margin-bottom: 5px;"> <tr><td>4</td><td>5</td></tr> <tr><td colspan="2" style="height: 15px;"></td></tr> </table> <p>D</p> </div> <div style="text-align: center;"> <table border="1" style="margin-bottom: 5px;"> <tr><td>5</td><td>6.5</td></tr> <tr><td colspan="2" style="height: 15px;"></td></tr> </table> <p>F</p> </div> <div style="text-align: center;"> <table border="1" style="margin-bottom: 5px;"> <tr><td>7</td><td>9.5</td></tr> <tr><td colspan="2" style="height: 15px;"></td></tr> </table> <p>H</p> </div> </div> <div style="display: flex; justify-content: space-around; align-items: flex-start; margin-top: 10px;"> <div style="text-align: center;"> <table border="1" style="margin-bottom: 5px;"> <tr><td>3</td><td>4.5</td></tr> <tr><td colspan="2" style="height: 15px;"></td></tr> </table> <p>C</p> </div> <div style="text-align: center;"> <table border="1" style="margin-bottom: 5px;"> <tr><td colspan="3" style="height: 15px;"></td></tr> <tr><td>14</td><td>13.5</td><td>10.5</td></tr> </table> <p>G</p> </div> </div> <p>Route = A – B – D – F – H Length = 9.5 miles</p>	1	0			6	8			2	2			4	5			5	6.5			7	9.5			3	4.5						14	13.5	10.5	<p>M1 Both 6 and 5 shown at <i>D</i> [5 may appear as perm label only] M1 14, 13.5 and 10.5 shown at <i>G</i> A1 No extra temporary labels All temporary labels correct [condone perm values only appearing as perm labels] [Dep on both M marks]</p> <p>B1 All permanent labels correct [may omit <i>G</i>, but if given it must be correct] B1 Order of labelling correct [may omit <i>G</i> but if given it must be correct]</p> <p>B1 cao B1 cao</p>	<p>[7]</p>
1	0																																				
6	8																																				
2	2																																				
4	5																																				
5	6.5																																				
7	9.5																																				
3	4.5																																				
14	13.5	10.5																																			
<p>(ii)</p>	<p>Route Inspection problem</p>	<p>B1</p>	<p>Accept Chinese Postman [1]</p>																																		
<p>(iii)</p>	<p>Odd nodes: <i>A, D, E</i> and <i>H</i> $AD = 5$ $AE = 8$ $AH = 9.5$ $EH = \frac{5}{10}$ $DH = \frac{4.5}{12.5}$ $DE = \frac{3.5}{13.0}$</p> <p>Repeat <i>AD</i> (<i>A-B-D</i>) and <i>EH</i> (<i>E-F-H</i>) Length = 67.5 + 10 = 77.5 miles</p>	<p>B1 Identifying or using <i>A, D, E, H</i> M1 Attempting at least one pairing A1 At least one correct pairing or correct total</p> <p>M1 Adding their 10 to 67.5 A1 77.5 (cao)</p>	<p>[5]</p>																																		
<p>(iv)</p>	<p>Repeat arcs <i>EF</i> and <i>FD</i> $3.5 + 67.5 = 71$ miles</p>	<p>B1 cao [NOT <i>DE</i> or <i>D-F-E</i>] B1 cao</p>	<p>[2]</p>																																		
<p>(v)</p>	<p><i>A – B – C – G – F – D</i> then method stalls <i>E</i> and <i>H</i> are missed out</p>	<p>B1</p>	<p>Showing route as far as <i>D</i> and then explaining the problem [1]</p>																																		
<p>(vi)</p>	<p><i>C – B – A – D – F – E – H – G – C</i> 37.5 miles</p>	<p>M1 [If final <i>C</i> is missing ⇒ M1, A0] A1 [A diagram needs arrows for A1] B1 37.5 (cao)</p>	<p>[3]</p>																																		
<p>(vii)</p>	<div style="text-align: center;"> </div> <p>Nodes: <i>B C D F E H G</i> Weight = 16 miles</p> <p>[Two shortest arcs from <i>A</i> are <i>AB</i> and <i>AD</i>] $2 + 6 + 16$ Lower bound = 24 miles</p>	<p>M1 A spanning tree on reduced network (may show <i>AB, AD</i>) A1 Correct minimum spanning tree marked, with no extra arcs</p> <p>B1 cao B1 cao</p> <p>M1 8 + their 16 (or implied) A1 cao</p>	<p>[6]</p>																																		
<p>Total = 25</p>																																					

<p>5 (i)</p>	<p>$15x+15y+30z \leq 9000$ [divide through by 15 to get $x+y+2z \leq 600$ as given] Stamping out: $5x+8y+10z \leq 3600$ Fixing pin: $50x+50y+50z \leq 25000$ $x + y + z \leq 500$ Checking: $100x+50y+20z \leq 10000$ $10x+5y+2z \leq 1000$</p>	<p>B1 B1 B1 B1</p>	<p>$15x+15y+30z \leq 9000$ $5x+8y+10z \leq 3600$ $x + y + z \leq 500$ $10x+5y+2z \leq 1000$</p>	<p>[4]</p>																																																																																										
<p>(ii)</p>	<p>x, y and z are non-negative</p>	<p>B1</p>	<p>$x \geq 0, y \geq 0$ and $z \geq 0$</p>	<p>[1]</p>																																																																																										
<p>(iii)</p>	<p>$(P =) 4x + 3y + z$</p>	<p>B1</p>	<p>cao</p>	<p>[1]</p>																																																																																										
<p>(iv)</p>	<table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <thead> <tr> <th>P</th> <th>x</th> <th>y</th> <th>z</th> <th>s</th> <th>t</th> <th>u</th> <th>v</th> <th>RHS</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>-4</td> <td>-3</td> <td>-1</td> <td>0</td> <td>0</td> <td>0</td> <td>0</td> <td>0</td> </tr> <tr> <td>0</td> <td>1</td> <td>1</td> <td>2</td> <td>1</td> <td>0</td> <td>0</td> <td>0</td> <td>600</td> </tr> <tr> <td>0</td> <td>5</td> <td>8</td> <td>10</td> <td>0</td> <td>1</td> <td>0</td> <td>0</td> <td>3600</td> </tr> <tr> <td>0</td> <td>1</td> <td>1</td> <td>1</td> <td>0</td> <td>0</td> <td>1</td> <td>0</td> <td>500</td> </tr> <tr> <td>0</td> <td>10</td> <td>5</td> <td>2</td> <td>0</td> <td>0</td> <td>0</td> <td>1</td> <td>1000</td> </tr> </tbody> </table>	P	x	y	z	s	t	u	v	RHS	1	-4	-3	-1	0	0	0	0	0	0	1	1	2	1	0	0	0	600	0	5	8	10	0	1	0	0	3600	0	1	1	1	0	0	1	0	500	0	10	5	2	0	0	0	1	1000	<p>B1 B1 M1 A1</p>	<p>Follow through if reasonable -4 -3 -1 in objective row Correct use of slack variables 1 1 2 and 600 correct All constraint rows correct Accept variations in order of rows and columns</p>	<p>[4]</p>																																				
P	x	y	z	s	t	u	v	RHS																																																																																						
1	-4	-3	-1	0	0	0	0	0																																																																																						
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0	5	8	10	0	1	0	0	3600																																																																																						
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0	10	5	2	0	0	0	1	1000																																																																																						
<p>(v)</p>	<p>Pivot on the 10 in the x-column</p> <table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <tbody> <tr><td>1</td><td>0</td><td>-1</td><td>-0.2</td><td>0</td><td>0</td><td>0</td><td>0.4</td><td>400</td></tr> <tr><td>0</td><td>0</td><td>0.5</td><td>1.8</td><td>1</td><td>0</td><td>0</td><td>-0.1</td><td>500</td></tr> <tr><td>0</td><td>0</td><td>5.5</td><td>9</td><td>0</td><td>1</td><td>0</td><td>-0.5</td><td>3100</td></tr> <tr><td>0</td><td>0</td><td>0.5</td><td>0.8</td><td>0</td><td>0</td><td>1</td><td>-0.1</td><td>400</td></tr> <tr><td>0</td><td>1</td><td>0.5</td><td>0.2</td><td>0</td><td>0</td><td>0</td><td>0.1</td><td>100</td></tr> </tbody> </table> <p>Pivot on 0.5 in the last row of y-column</p> <table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <tbody> <tr><td>1</td><td>2</td><td>0</td><td>0.2</td><td>0</td><td>0</td><td>0</td><td>0.6</td><td>600</td></tr> <tr><td>0</td><td>-1</td><td>0</td><td>1.6</td><td>1</td><td>0</td><td>0</td><td>-0.2</td><td>400</td></tr> <tr><td>0</td><td>-11</td><td>0</td><td>6.8</td><td>0</td><td>1</td><td>0</td><td>-1.6</td><td>2000</td></tr> <tr><td>0</td><td>-1</td><td>0</td><td>0.6</td><td>0</td><td>0</td><td>1</td><td>-0.2</td><td>300</td></tr> <tr><td>0</td><td>2</td><td>1</td><td>0.4</td><td>0</td><td>0</td><td>0</td><td>0.2</td><td>200</td></tr> </tbody> </table> <p>$x = 0, y = 200, z = 0, P = 600$ Make 20000 metallic badges (and no laminated badges or plastic badges) To give a profit of £600 6000 seconds (100 min) of printing time not used, 2000 seconds (33 min 20 sec) of stamping out time not used, 15000 seconds (250 min) of fixing pin time not used. All the checking time is used</p>	1	0	-1	-0.2	0	0	0	0.4	400	0	0	0.5	1.8	1	0	0	-0.1	500	0	0	5.5	9	0	1	0	-0.5	3100	0	0	0.5	0.8	0	0	1	-0.1	400	0	1	0.5	0.2	0	0	0	0.1	100	1	2	0	0.2	0	0	0	0.6	600	0	-1	0	1.6	1	0	0	-0.2	400	0	-11	0	6.8	0	1	0	-1.6	2000	0	-1	0	0.6	0	0	1	-0.2	300	0	2	1	0.4	0	0	0	0.2	200	<p>B1 M1 A1 B1 M1 A1 B1 B1 B1</p>	<p>Correct choice of pivot from x- column [Follow through their tableau and valid pivot if possible: no negative values in RHS column and P value has not decreased] Pivot row correct Other rows correct Correct choice of pivot from y-column [Follow through their tableau and valid pivot if possible] Pivot row correct Other rows correct Interpretation of their x, y and z values in context (may imply zero entries) Interpretation of their P value in context Interpretation of their slack variable values</p>	<p>[3] [3] [3]</p>
1	0	-1	-0.2	0	0	0	0.4	400																																																																																						
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0	1	0.5	0.2	0	0	0	0.1	100																																																																																						
1	2	0	0.2	0	0	0	0.6	600																																																																																						
0	-1	0	1.6	1	0	0	-0.2	400																																																																																						
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0	2	1	0.4	0	0	0	0.2	200																																																																																						
<p>Total = 19</p>																																																																																														