

4730

Mark Scheme

June 2010

<p>1</p>	<p>For included angle marked α or for $0.8(10.5 - 8.5\cos\alpha) = 4\cos\beta$ For opposite side marked 4/0.8 (or 4) or for $- 0.8 \times 8.5 \sin\alpha = 4\sin\beta$</p> <p>$8.4^2 + 6.8^2 - 2 \times 8.4 \times 6.8 \cos\alpha = 4^2$ $\alpha = 28.1^\circ$</p>	<p>M1 A1 A1 M1 A1ft A1 [6]</p>	<p>For triangle with two of its sides marked 0.8 x 10.5 and 0.8 x 8.5 (or 10.5 and 8.5) or for using $I = \Delta mv$ in one direction.</p> <p>Allow B1 for omission of 0.8</p> <p>Allow B1 for omission of 0.8 For using the cosine rule or for eliminating β ft 0.8 mis-used or not used</p>
<p>2(i)</p>	<p>[$100a = 2aV_B$] Vertical component at B is 50 N Vertical component at C is 150 N</p>	<p>M1 A1 A1 [3]</p>	<p>For taking moments about A for AB</p>
<p>(ii)</p>	<p>$100(0.5a) + (\sqrt{3} a)F = 150a$ or $100a + 100(1.5a) = 150a + (\sqrt{3} a)F$ Frictional force is 57.7 N Direction is to the right</p>	<p>M1 A1ft A1 B1 [4]</p>	<p>For taking moments about B for BC (3 terms needed) or about A for the whole (4 terms needed)</p>
<p>3(i)</p>	<p>$u = 4$ $v = 2$</p>	<p>B1 B1 [2]</p>	
<p>(ii)</p>	<p>$mu = ma + mb$ (or $u = b - a$) $u = b - a$ (or $mu = ma + mb$) $a = 0$ and $b = 4\text{ms}^{-1}$ Speed of A is 2ms^{-1} and direction at 90° to the wall Speed of B is 4ms^{-1} and direction parallel to the wall</p>	<p>M1 A1 B1 A1ft A1ft A1ft [6]</p>	<p>For using the principle of conservation of momentum or for using NEL with $e = 1$</p> <p>ft incorrect u</p> <p>ft incorrect v</p> <p>ft incorrect u</p>
<p>4(i)</p>	<p>[$0.25 \text{ dv/dt} = 3/50 - t^2/2400$]</p> <p>$v = 12t/50 - t^3/1800$ $[v(12) = 1.92]$ $[0.25 \text{ dv/dt} = t^2/2400 - 3/50 \rightarrow$ $v = t^3/1800 - 12t/50 + C_2]$ $[1.92 = 0.96 - 2.88 + C_2]$ $v = t^3/1800 - 12t/50 + 3.84$ $v(24) = 5.76 = 3 \times v(12)$</p>	<p>M1 M1 A1 M1 M1 M1 A1 A1 [8]</p>	<p>For using Newton's second law (1st or 2nd stage) For attempting to integrate (1st stage) and using $v(0) = 0$ (may be implied by the absence of $+ C_1$)</p> <p>For evaluating v when force is zero For using Newton's second law (2nd stage) and integrating For using $v(12) = 1.92$</p> <p>AG</p>

(ii)	Sketch has $v(0) = 0$ and slope decreasing (convex upwards) for $0 < t < 12$ Sketch has slope increasing (concave upwards) for $12 < t < 24$ Sketch has $v(t)$ continuous, single valued and increasing (except possibly at $t = 12$) with $v(24)$ seen to be $> 2v(12)$	B1 B1 B1 [3]	
5(i)	For using amplitude as a coefficient of a relevant trigonometric function. For using the value of ω as a coefficient of t in a relevant trigonometric function. $x_1 = 3\cos t$ and $x_2 = 4\cos 1.5t$	B1 B1 B1 [3]	
(ii)	Part distance is 20m $[20 - (-3.62)]$ Distance travelled by P_2 is 23.6 m	M1 A1 M1 A1 [4]	For using distance travelled by P_2 for $0 < t < 5\pi/3$ is $5A_2$ For subtracting displacement of P_2 when $t = 5.99$ from part distance.
(iii)	$\dot{x}_1 = -3\sin t$; $\dot{x}_2 = -6\sin 1.5t$ $v_1 = 0.867$, $v_2 = -2.55$; opposite directions	M1 A1 M1 A1 [4]	For differentiating x_1 and x_2 For evaluating when $t = 5.99$ (must use radians)
	Alternative for (iii): $v_1^2 = 3^2 - 2.87^2$, $v_2^2 = 2.25[4^2 - (-3.62)^2]$ $[\pi < 5.99 < 2\pi \rightarrow v_1 > 0$, $4\pi/3 < 5.99 < 2\pi \rightarrow v_2 < 0]$ $v_1 = 0.867$, $v_2 = -2.55$; opposite directions	M1 A1 M1 A1	For using $v^2 = n^2(a^2 - x^2)$ (must use radians to find values of x) For using the idea that v starts -ve and changes sign at intervals of $T/2$ s
6(i)	PE loss at lowest allowable point = 25W EE gain = $32000x^2/(2 \times 20)$ $[25W = 20000]$ Value of W is 800	B1 M1 A1 M1 A1 [5]	For using $EE = \lambda x^2/(2L)$; may be scored in (i) or in (ii) For equating PE loss and EE gain and attempting to solve for W
(ii)	$[800 = 32000x/20]$ $\frac{1}{2} (800/9.8)v^2$ $= 800 \times 20.5 - 32000x0.5^2/(2 \times 20)$ Maximum speed is 19.9ms^{-1}	M1 M1 A1 A1 [4]	For using $W = \lambda x/L$ at max speed For using the principle of conservation of energy (3 terms required)
(iii)	$(800) \ddot{x}/g = 800 - 32000 \times 5/20$ Max. deceleration is 88.2ms^{-2}	M1 A1 A1 [3]	For applying Newton's second law to jumper at lowest point (3 terms needed)

4730

Mark Scheme

June 2010

<p>7(i)</p>	<p>$[\frac{1}{2}mv^2 - \frac{1}{2}m6^2 = mg(0.7)]$ Speed of P before collision is 7.05ms^{-1} Coefficient of restitution is 0.695</p>	<p>M1 A1 B1ft [3]</p>	<p>For using the principle of conservation of energy for P (3 terms needed) ft $4.9 \div$ speed of P before collision</p>
<p>(ii)</p>	<p>$[\frac{1}{2}mv^2 = \frac{1}{2}m4.9^2 - mg0.7(1 - \cos\theta)]$ $v^2 = 3.43(3 + 4\cos\theta)$ $T - mg\cos\theta = mv^2/0.7$ $[T - m9.8\cos\theta = m3.43(3 + 4\cos\theta)/0.7]$ Tension is $14.7m(1 + 2\cos\theta)$ N</p>	<p>M1 A1 M1 A1 M1 A1 [6]</p>	<p>For using the principle of conservation of energy for Q Accept any correct form For using Newton's second law radially with $a_r = v^2/r$ For substituting for v^2 AG</p>
<p>(iii)</p>	<p>$T = 0 \rightarrow \theta = 120^\circ$ Radial acceleration is $(\pm)4.9\text{ms}^{-1}$ or transverse acceleration is $(\pm)8.49\text{ms}^{-1}$ Radial acceleration is $(\pm)4.9\text{ms}^{-1}$ and transverse acceleration is $(\pm)8.49\text{ms}^{-1}$</p>	<p>B1 M1 A1 B1 [4]</p>	<p>For using $a_r = -g\cos\theta$ $\{ \text{or } 3.43(3 + 4\cos\theta)/0.7 \}$ or $a_t = -g\sin\theta$</p>
			<p>SR for candidates with a sin/cos mix in the work for M1 A1 B1 immediately above. (max. 1/3) Radial acceleration is $(\pm)8.49\text{ms}^{-1}$ and transverse acceleration is $(\pm)4.9\text{ms}^{-1}$ B1</p>
<p>(iv)</p>	<p>$[V^2 = 3.43\{3 + 4(-0.5)\}x0.5^2 \text{ or } V^2 = (-g\cos120^\circ x 0.7) x \cos^260^\circ]$ $V^2 = 0.8575$ $[mgH = \frac{1}{2}m(4.9^2 - 0.8575) \text{ or } mg(H - 1.05) = \frac{1}{2}m(3.43 - 0.8575)]$ Greatest height is 1.18 m</p>	<p>M1 A1 M1 A1 [4]</p>	<p>For using $V = v(120^\circ) x \cos60^\circ$ AG For using the principle of conservation of energy</p>