



1. Sammy is studying the number of units of gas,  $g$ , and the number of units of electricity,  $e$ , used in her house each week. A random sample of 10 weeks use was recorded and the data for each week were coded so that  $x = \frac{g - 60}{4}$  and  $y = \frac{e}{10}$ . The results for the coded data are summarised below

$$\sum x = 48.0 \quad \sum y = 58.0 \quad S_{xx} = 312.1 \quad S_{yy} = 2.10 \quad S_{xy} = 18.35$$

- (a) Find the equation of the regression line of  $y$  on  $x$  in the form  $y = a + bx$ .

Give the values of  $a$  and  $b$  correct to 3 significant figures.

(4)

- (b) Hence find the equation of the regression line of  $e$  on  $g$  in the form  $e = c + dg$ .

Give the values of  $c$  and  $d$  correct to 2 significant figures.

(4)

- (c) Use your regression equation to estimate the number of units of electricity used in a week when 100 units of gas were used.

(2)

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3. An agriculturalist is studying the yields,  $y$  kg, from tomato plants. The data from a random sample of 70 tomato plants are summarised below.

Yield ( $y$ kg)	Frequency ( $f$ )	Yield midpoint ( $x$ kg)
$0 \leq y < 5$	16	2.5
$5 \leq y < 10$	24	7.5
$10 \leq y < 15$	14	12.5
$15 \leq y < 25$	12	20
$25 \leq y < 35$	4	30

(You may use  $\sum fx = 755$  and  $\sum fx^2 = 12037.5$ )

A histogram has been drawn to represent these data.

The bar representing the yield  $5 \leq y < 10$  has a width of 1.5 cm and a height of 8 cm.

- (a) Calculate the width and the height of the bar representing the yield  $15 \leq y < 25$  (3)
- (b) Use linear interpolation to estimate the median yield of the tomato plants. (2)
- (c) Estimate the mean and the standard deviation of the yields of the tomato plants. (4)
- (d) Describe, giving a reason, the skewness of the data. (2)
- (e) Estimate the number of tomato plants in the sample that have a yield of more than 1 standard deviation above the mean. (2)

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4. The time, in minutes, taken to fly from London to Malaga has a normal distribution with mean 150 minutes and standard deviation 10 minutes.

- (a) Find the probability that the next flight from London to Malaga takes less than 145 minutes. (3)

The time taken to fly from London to Berlin has a normal distribution with mean 100 minutes and standard deviation  $d$  minutes.

Given that 15% of the flights from London to Berlin take longer than 115 minutes,

- (b) find the value of the standard deviation  $d$ . (4)

The time,  $X$  minutes, taken to fly from London to another city has a normal distribution with mean  $\mu$  minutes.

Given that  $P(X < \mu - 15) = 0.35$

- (c) find  $P(X > \mu + 15 \mid X > \mu - 15)$ . (3)

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5. A researcher believes that parents with a short family name tended to give their children a long first name. A random sample of 10 children was selected and the number of letters in their family name,  $x$ , and the number of letters in their first name,  $y$ , were recorded.

The data are summarised as:

$$\sum x = 60, \quad \sum y = 61, \quad \sum y^2 = 393, \quad \sum xy = 382, \quad S_{xx} = 28$$

- (a) Find  $S_{yy}$  and  $S_{xy}$  **(3)**
- (b) Calculate the product moment correlation coefficient,  $r$ , between  $x$  and  $y$ . **(2)**
- (c) State, giving a reason, whether or not these data support the researcher's belief. **(2)**

The researcher decides to add a child with family name "Turner" to the sample.

- (d) Using the definition  $S_{xx} = \sum (x - \bar{x})^2$ , state the new value of  $S_{xx}$  giving a reason for your answer. **(2)**

Given that the addition of the child with family name "Turner" to the sample leads to an increase in  $S_{yy}$

- (e) use the definition  $S_{xy} = \sum (x - \bar{x})(y - \bar{y})$  to determine whether or not the value of  $r$  will increase, decrease or stay the same. Give a reason for your answer. **(2)**

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6.

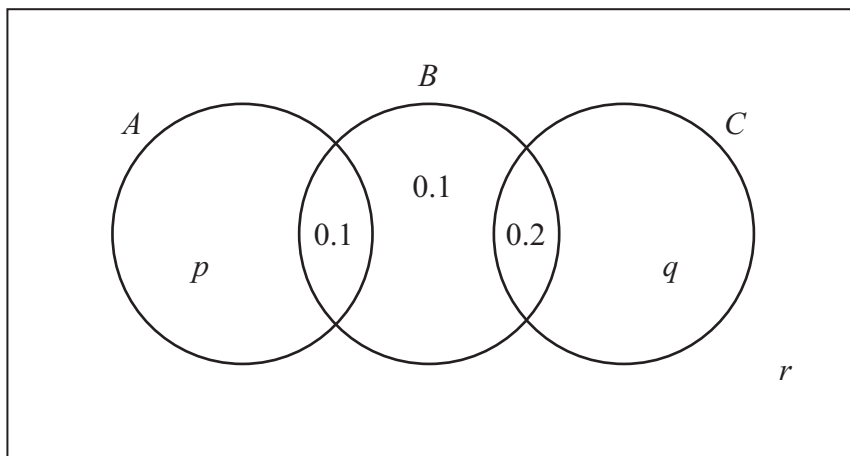


Figure 1

The Venn diagram in Figure 1 shows three events  $A$ ,  $B$  and  $C$  and the probabilities associated with each region of  $B$ . The constants  $p$ ,  $q$  and  $r$  each represent probabilities associated with the three separate regions outside  $B$ .

The events  $A$  and  $B$  are independent.

(a) Find the value of  $p$ . (3)

Given that  $P(B|C) = \frac{5}{11}$

(b) find the value of  $q$  and the value of  $r$ . (4)

(c) Find  $P(A \cup C|B)$ . (2)

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7. The score  $S$  when a spinner is spun has the following probability distribution.

$s$	0	1	2	4	5
$P(S = s)$	0.2	0.2	0.1	0.3	0.2

- (a) Find  $E(S)$ . (2)
- (b) Show that  $E(S^2) = 10.4$  (2)
- (c) Hence find  $\text{Var}(S)$ . (2)
- (d) Find
  - (i)  $E(5S - 3)$ ,
  - (ii)  $\text{Var}(5S - 3)$ . (4)
- (e) Find  $P(5S - 3 > S + 3)$  (3)

The spinner is spun twice.

The score from the first spin is  $S_1$  and the score from the second spin is  $S_2$

The random variables  $S_1$  and  $S_2$  are independent and the random variable  $X = S_1 \times S_2$

- (f) Show that  $P(\{S_1 = 1\} \cap X < 5) = 0.16$  (2)
- (g) Find  $P(X < 5)$ . (3)

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