



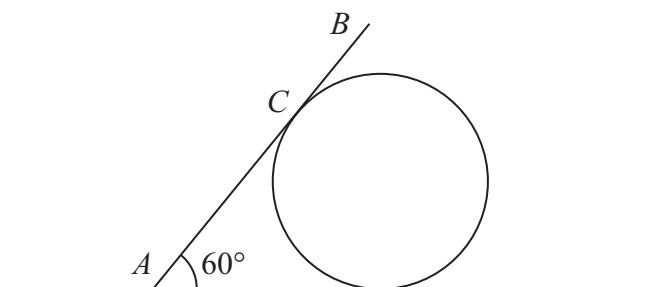








4. A rough circular cylinder of radius  $4a$  is fixed to a rough horizontal plane with its axis horizontal. A uniform rod  $AB$ , of weight  $W$  and length  $6a\sqrt{3}$ , rests with its lower end  $A$  on the plane and a point  $C$  of the rod against the cylinder. The vertical plane through the rod is perpendicular to the axis of the cylinder. The rod is inclined at  $60^\circ$  to the horizontal, as shown in Figure 1.



**Figure 1**

- (a) Show that  $AC = 4a\sqrt{3}$  (2)

The coefficient of friction between the rod and the cylinder is  $\frac{\sqrt{3}}{3}$  and the coefficient of friction between the rod and the plane is  $\mu$ . Given that friction is limiting at both  $A$  and  $C$ ,

- (b) find the value of  $\mu$ . (9)

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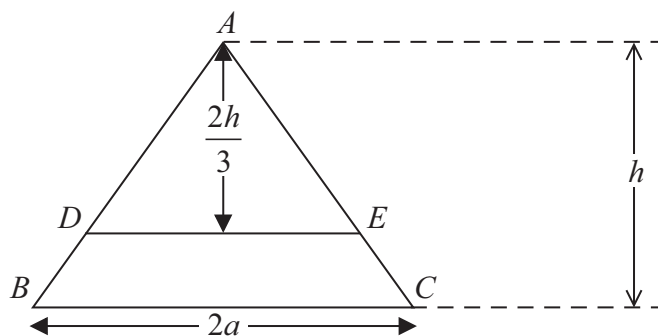


Figure 2

A uniform triangular lamina  $ABC$  of mass  $M$  is such that  $AB = AC$ ,  $BC = 2a$  and the distance of  $A$  from  $BC$  is  $h$ . A line, parallel to  $BC$  and at a distance  $\frac{2h}{3}$  from  $A$ , cuts  $AB$  at  $D$  and cuts  $AC$  at  $E$ , as shown in Figure 2.

It is given that the mass of the trapezium  $BCED$  is  $\frac{5M}{9}$ .

- (a) Show that the centre of mass of the trapezium  $BCED$  is  $\frac{7h}{45}$  from  $BC$ . (5)

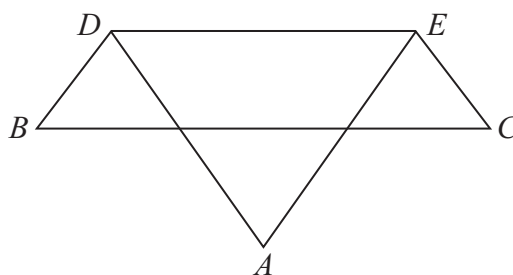


Figure 3

The portion  $ADE$  of the lamina is folded through  $180^\circ$  about  $DE$  to form the folded lamina shown in Figure 3.

- (b) Find the distance of the centre of mass of the folded lamina from  $BC$ . (4)

The folded lamina is freely suspended from  $D$  and hangs in equilibrium. The angle between  $DE$  and the downward vertical is  $\alpha$ .

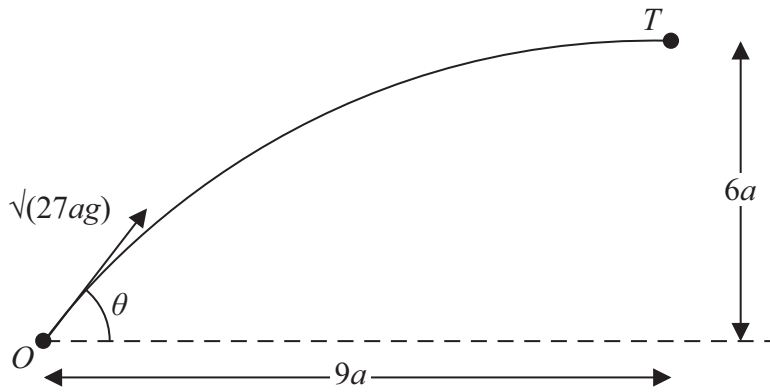
- (c) Find  $\tan \alpha$  in terms of  $a$  and  $h$ . (4)







7.



**Figure 4**

A small ball is projected from a fixed point  $O$  so as to hit a target  $T$  which is at a horizontal distance  $9a$  from  $O$  and at a height  $6a$  above the level of  $O$ . The ball is projected with speed  $\sqrt{27ag}$  at an angle  $\theta$  to the horizontal, as shown in Figure 4. The ball is modelled as a particle moving freely under gravity.

- (a) Show that  $\tan^2 \theta - 6 \tan \theta + 5 = 0$  **(7)**

The two possible angles of projection are  $\theta_1$  and  $\theta_2$ , where  $\theta_1 > \theta_2$ .

- (b) Find  $\tan \theta_1$  and  $\tan \theta_2$ . **(3)**

The particle is projected at the larger angle  $\theta_1$ .

- (c) Show that the time of flight from  $O$  to  $T$  is  $\sqrt{\left(\frac{78a}{g}\right)}$ . **(3)**

- (d) Find the speed of the particle immediately before it hits  $T$ . **(3)**

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